

**Quiz 6 for Statistics 301**  
**Elementary Statistical Methods - Spring 1999**  
**Material Covered: Chapter 12 of Workbook; Chapter 9 of text**  
**For: 16th April**

Name (please print): \_\_\_\_\_  
last first

Octane ratings from a supplier's pipeline were sampled on 12 consecutive days. Assume the octane ratings follow a normal distribution.

88.6, 86.6, 89.6, 87.6, 88.3, 88.8,  
88.9, 87.4, 87.9, 88.0, 88.2, 88.5,

1. [1] Give the p-value that demonstrates whether or not the data supports the claim the average octane rating is greater than 87.5. \_\_\_\_\_.
2. [2] In a second independent sample of 15 octane ratings, we find  $\bar{x}_2 = 88.5$ ,  $s_2 = 0.43$ . We are interested in testing whether or not the average difference in octane ratings is the same or different at a level of significance of 5%. In particular, the p-value is (do *not* pool) \_\_\_\_\_.
3. [2] In a second independent sample of 17 octane ratings, we find  $\bar{x}_2 = 87.5$ ,  $s_2 = 0.53$ .  
The standard error is (pool) \_\_\_\_\_.
4. [1] We are interested in testing whether or not the percentage of octane ratings between 88.0 and 88.9 (including 88.0 and 88.9) is less than 60%. The p-value is \_\_\_\_\_.

1. Determine the following probability and percentile.

(a) [1]  $P(-2.31 < t_{14} < 0.32) = \mathbf{0.60}$

(b) [1] 23rd percentile of  $t_7$   $\mathbf{-0.78}$

2. Octane ratings from a supplier's pipeline were sampled on 12 consecutive days. Assume the octane ratings follow a normal distribution.

88.6, 86.6, 89.6, 87.6, 88.3, 88.8,  
88.9, 87.4, 87.9, 88.0, 88.2, 88.5,

(a) [1] The 95% confidence interval for the average octane rating is (87.7, 88.7)

(b) [1] Give the p-value that demonstrates whether or not the data supports the claim the average octane rating is greater than 87.5. p-value =  $P(\bar{X} > 87.5) \approx 0.005$

3. A parcel delivery service requires that the standard deviation in fees charged not exceed \$2. In a random sample of 33 deliveries, it was found that  $s = \$2.12$ .

(a) [1] The statement of the test, in this case, is  $H_o : \sigma = 2$  versus  $H_a : \sigma < 2$

(b) [1] The observed value of the  $\chi^2$  test statistic is  $\frac{(n-1)s^2}{\sigma^2} \approx 35.976$